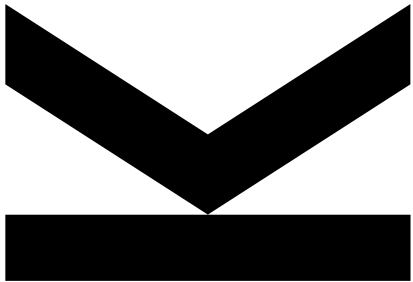


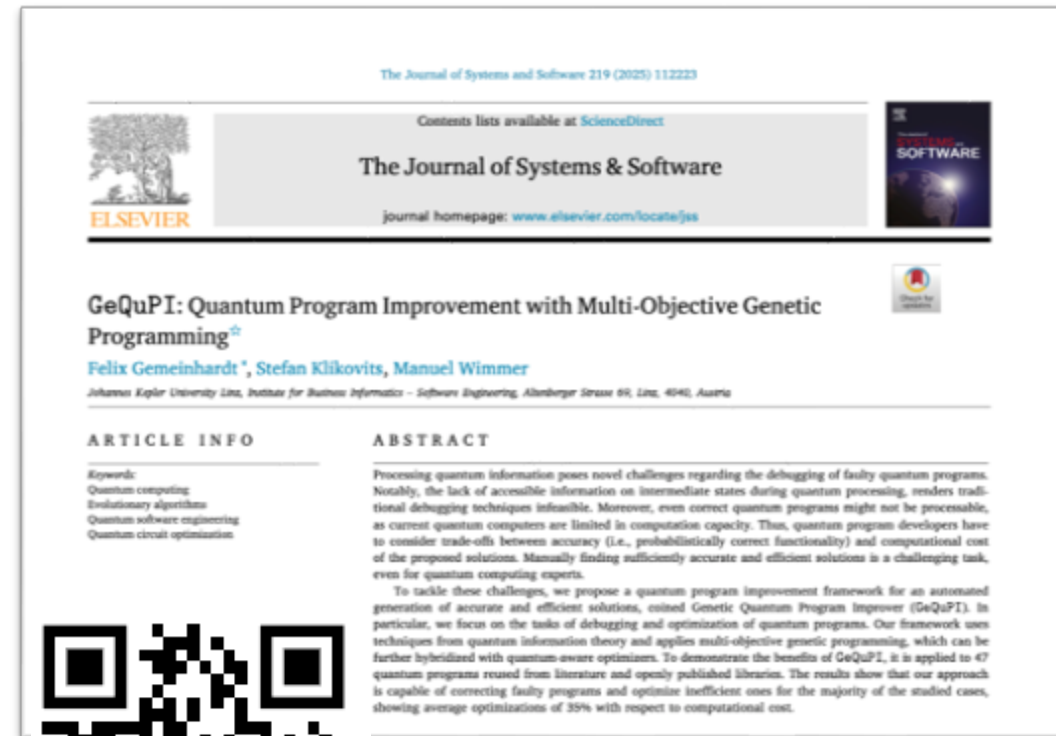
**JKU**

**JOHANNES KEPLER  
UNIVERSITY LINZ**

# GeQuPI: Quantum Program Improvement with Multi-Objective Genetic Programming



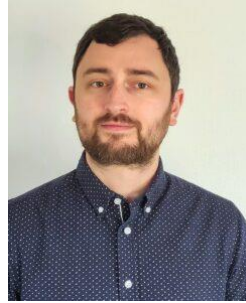
F. Gemeinhardt, S. Klikovits, M. Wimmer  
Institute of Business Informatics – Software Engineering (BISE)



# Quantum Software Team at BISE



Felix Gemeinhardt



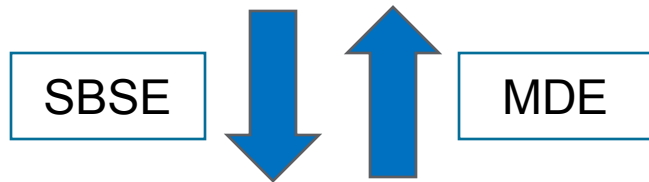
Stefan Klikovits



Manuel Wimmer  
(Head)



Christoph Stein

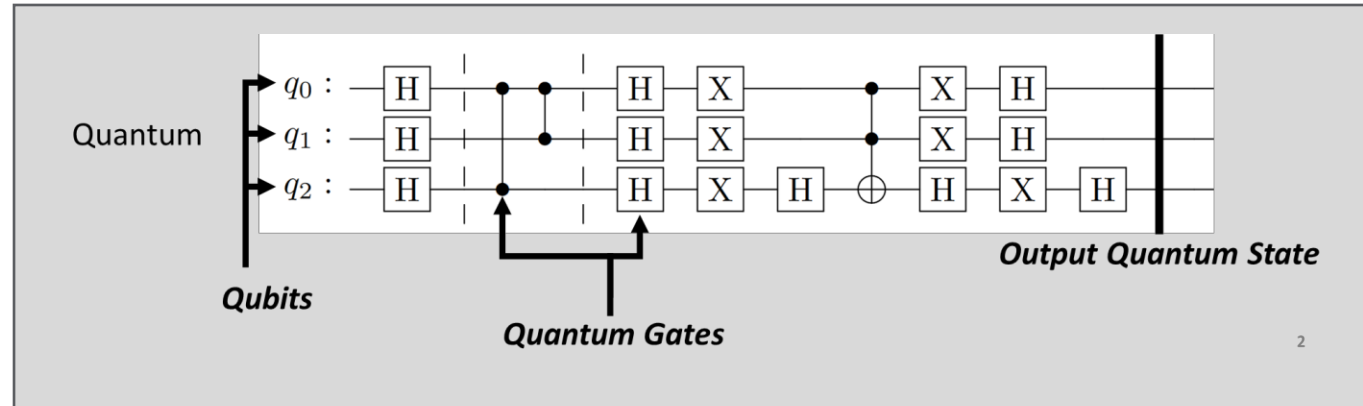


## Research Focus: Automated Quantum Software Engineering

- Direction I: Model-Driven Quantum Software Engineering
- **Direction II: Search-Based Quantum Software Engineering**

# Context & Problem Setting

## Quantum Circuits



## Challenges

- Vast design space
- Precision vs. computational cost
- Errors, Probabilistic Nature & NISQ

# Search-Based Software Engineering

Extensively used for classical software systems for about two decades [Harman et al. 2012]

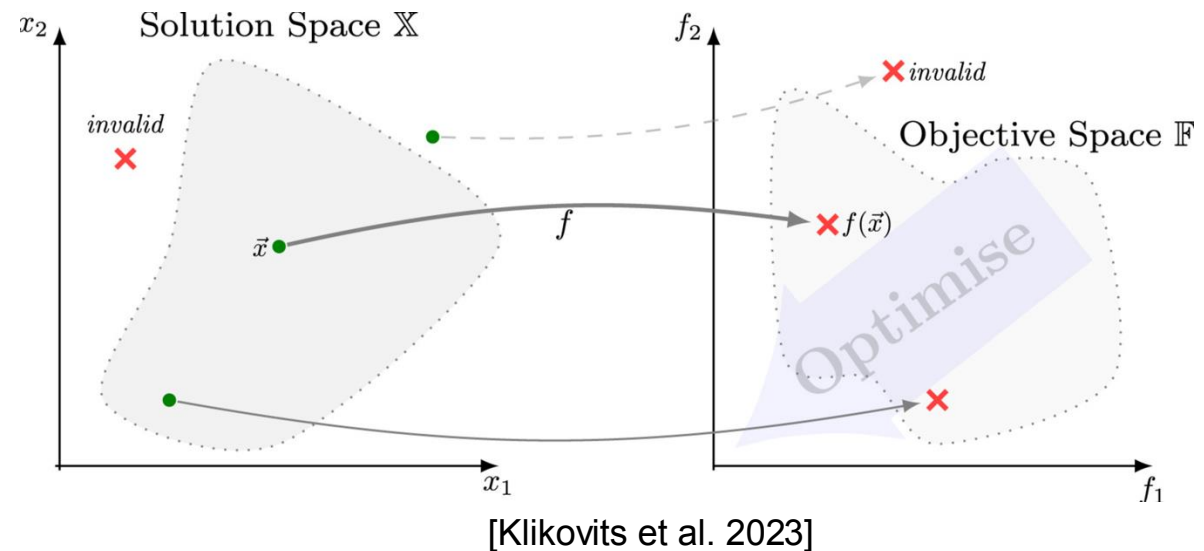
Goal: Find a software system / program that will optimize a given fitness function

## Advantages:

- Automated exploration by
- Meta-heuristic searchers  
Genetic Programming (GP), ...

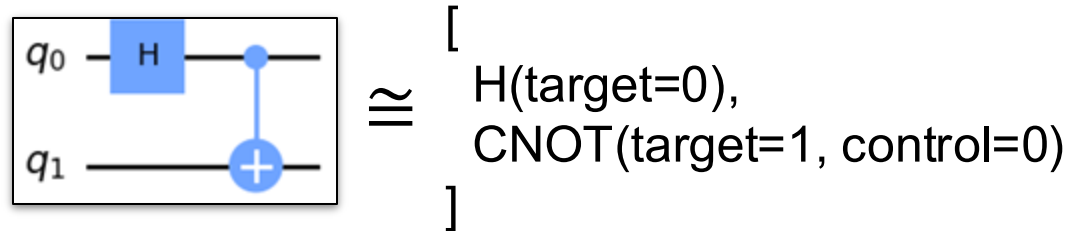
## Challenges: Find a good

1. Program encoding
2. Fitness function



# Typical GP Setup for Quantum Circuits

## Encoding: gate vector



## Fitness

behaviour: accuracy, and  
structure: # gates, depth,  
# non-local gates, # parameters

## Operators

mutation: add / delete / move / alter / swap gate  
change qubits, ...  
crossover: one-point, two-point, ...  
selection: tournament, ...

## Algorithms

use of classical meta-heuristic algorithms:  
GA, NSGA-II, NSGA-III, ...

Is this all we need?

# Using GP for QSE (1): Synthesis

GP4QSE

Circuit Synthesis

Operator Synthesis

[Gemeinhardt et al. 2023]

## Hybrid Multi-Objective Genetic Programming for Parameterized Quantum Operator Discovery

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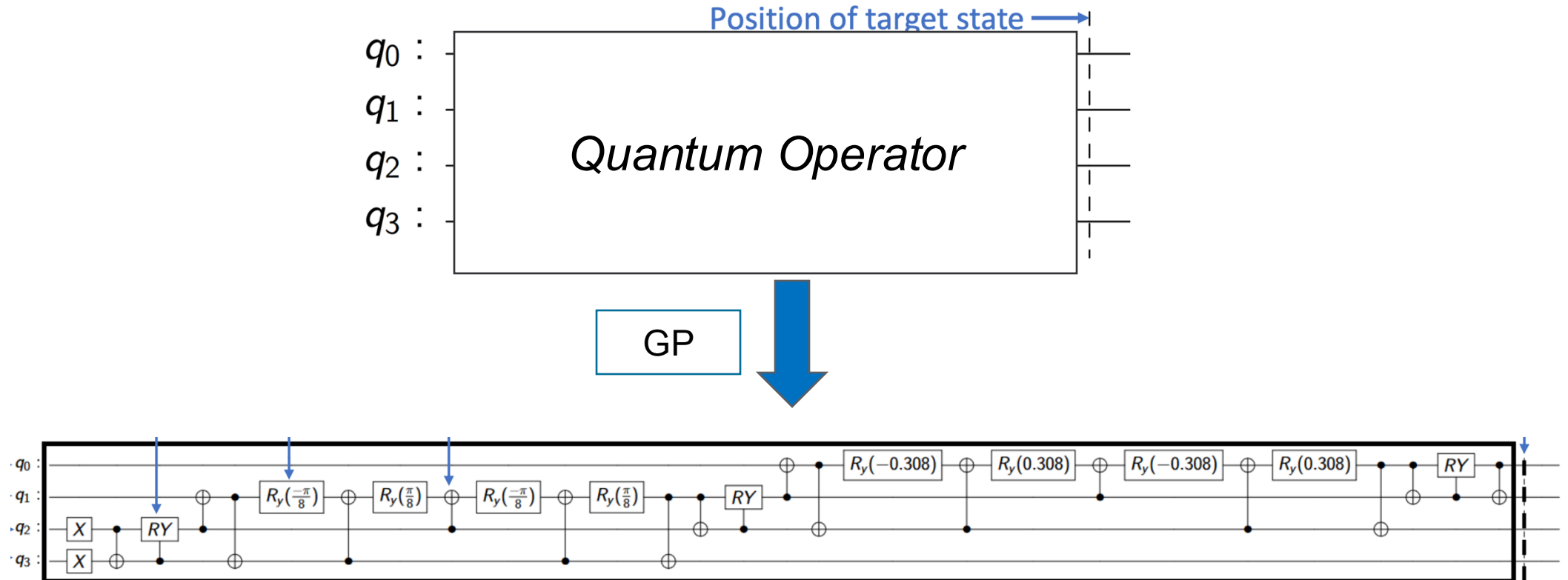
### ABSTRACT

The processing of quantum information is defined by quantum circuits. For applications on current quantum devices, these are usually parameterized, i.e., they contain operations with variable parameters. The design of such quantum circuits and aggregated higher-level quantum operators is a challenging task which requires significant knowledge in quantum information theory, provided a polynomial-sized solution can be found analytically at all. Moreover, finding an accurate solution with low computational cost represents a significant trade-off, particularly for the current generation of quantum computers. To tackle these challenges, we propose a multi-objective genetic programming approach—hybridized with a numerical parameter optimizer—to automate the synthesis of parameterized quantum operators. To demonstrate the benefits of the proposed approach, it is applied to a quantum circuit of a hybrid quantum-classical algorithm, and then compared to an analytical solution as well as a non-hybrid version. The results show that

### 1 INTRODUCTION

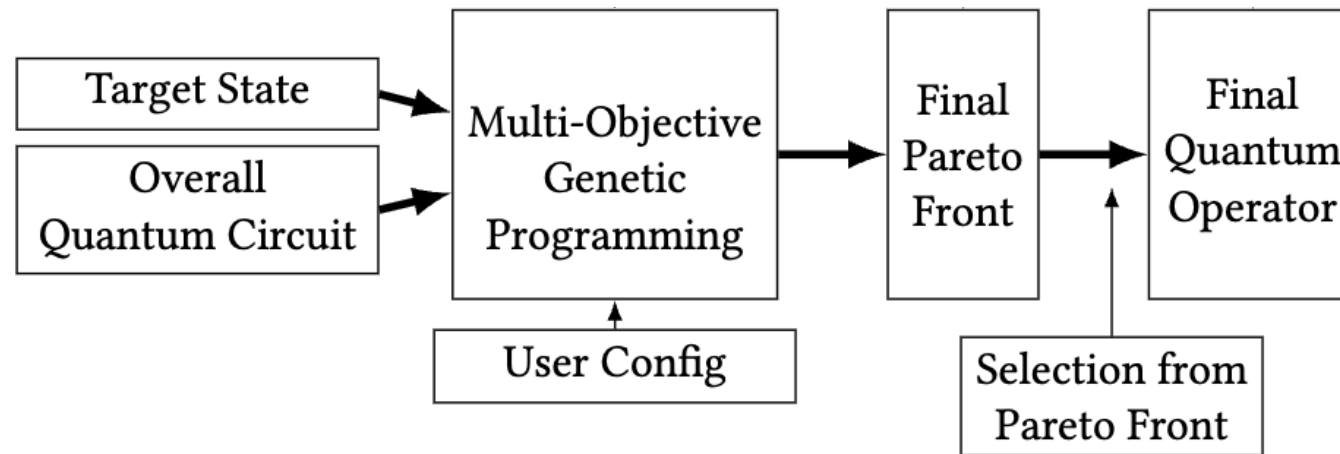
*Quantum Computing.* The current era of *Quantum Computing* (QC) is referred to as the *Noisy Intermediate-Scale Quantum* (NISQ) era, where the limitations of quantum hardware are mitigated by significant means of classical computation [16]. Analogously to logic gates for classical computation, in QC, quantum information is processed with operations called quantum gates. The most commonly used realistic model of QC is the so-called quantum circuit model [14]. Quantum gates can be parameterized, where the use of parameterized quantum circuits is common in the NISQ-era. This is because classical optimization of the parameters, which constitutes an NP-hard problem, allows to cope with the noise present in current quantum hardware [3]. For this reason, numerical parameter optimizers constitute a central element of NISQ-era quantum algorithms [3–5]. There is ongoing research on quantum-aware optimizers, which are particularly capable of coping with specific requirements of parameterized quantum circuits [3–5, 12].

# Scenario 1 – Operator Synthesis





# Our Approach: Search Scheme using GP

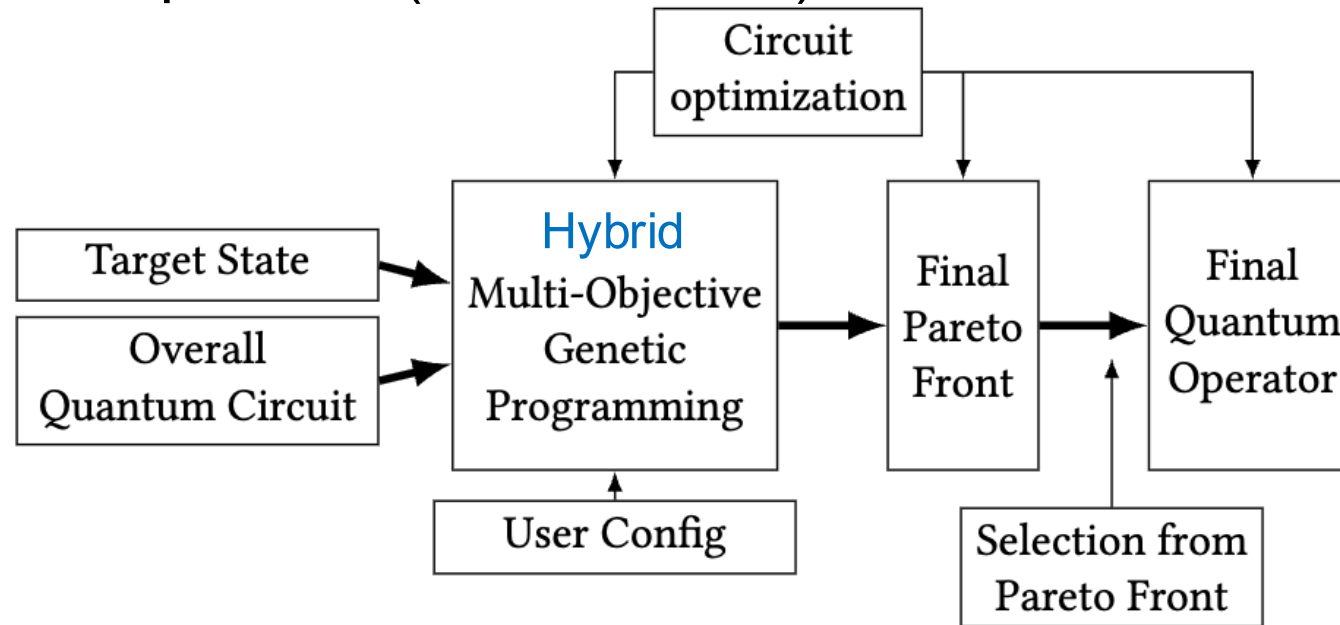


# Our Approach: Search Scheme using GP

**Problem:** Some gates (e.g.,  $RX_\theta, RY_\theta, RZ_\theta$ ) require **parameters**  $\theta \in (0, 2\pi)$

**Solution:** Use Hybrid Search Scheme

– Apply parameter optimizer (Nelder-Mead) inside GP



# Experimental Evaluation

**RQ1:** Hybrid vs Non-Hybrid - **diversity**?

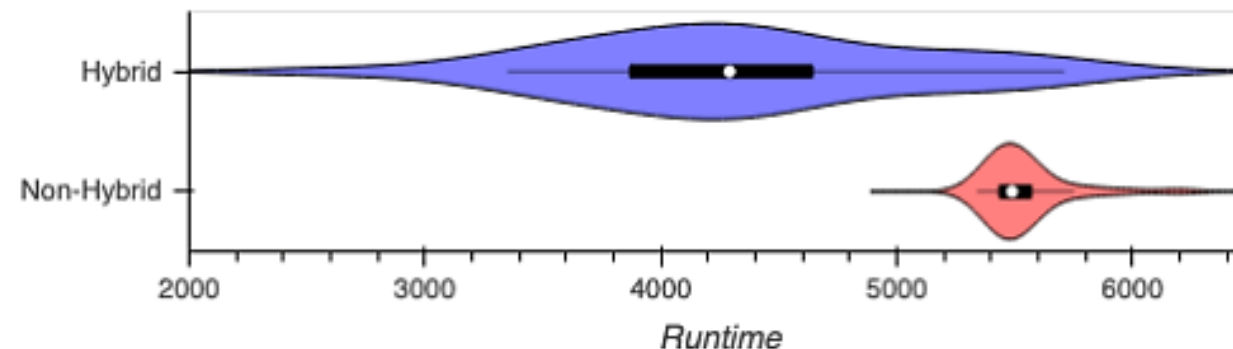
**RQ2:** Hybrid vs Non-Hybrid - **accuracy** (i.e., overlap)?

**RQ3:** Hybrid vs Non-Hybrid vs. Analytical Solution?

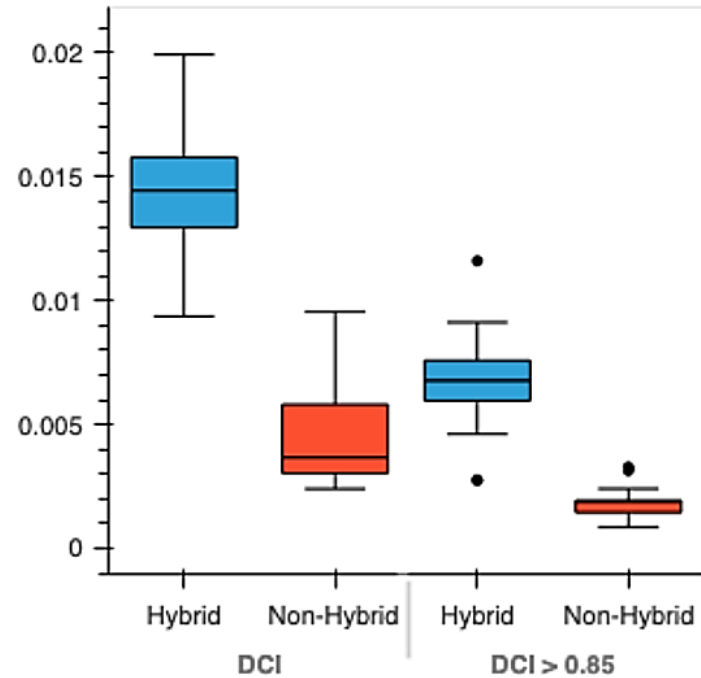
Selected Case: **GM-QAOA** [Bärtschi and Eidenbenz 2020]

Meta-heuristic search algorithm: NSGA-III

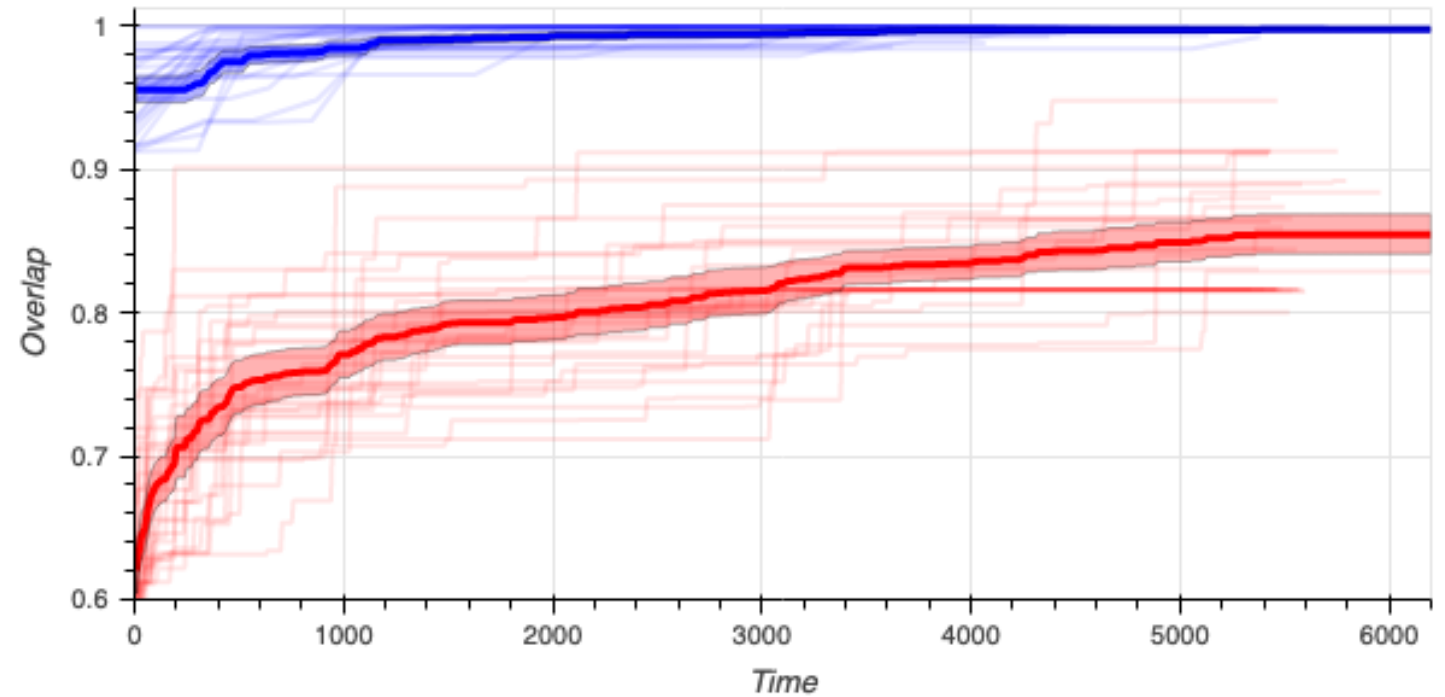
Implementation: Deap, Qiskit



# Results



RQ1: better diversity



RQ2: Hybrid has higher overlap  
+ faster convergence

# Using GP for QSE (2): Improvement

GP4QSE

Circuit Improvement

Optimization    Debugging  
[Gemeinhardt et al. 2025]

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## GeQuPI: Quantum Program Improvement with Multi-Objective Genetic Programming<sup>☆</sup>

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### ARTICLE INFO

**Keywords:**  
Quantum computing  
Evolutionary algorithms  
Quantum software engineering  
Quantum circuit optimization

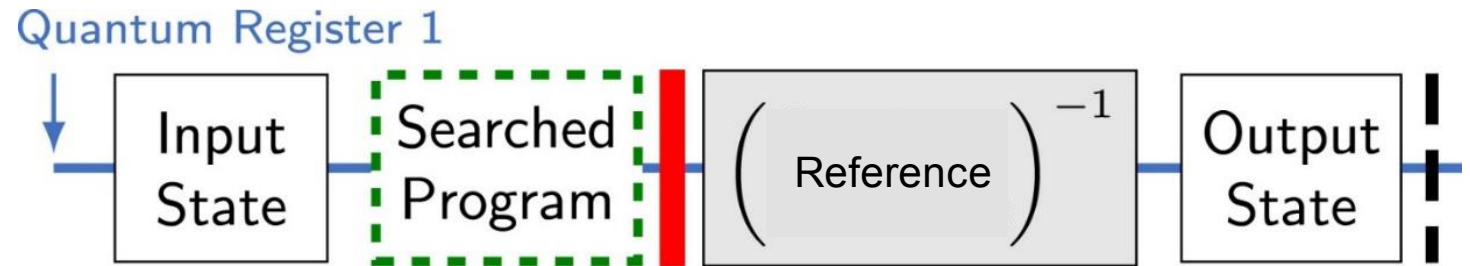
### ABSTRACT

Processing quantum information poses novel challenges regarding the debugging of faulty quantum programs. Notably, the lack of accessible information on intermediate states during quantum processing, renders traditional debugging techniques infeasible. Moreover, even correct quantum programs might not be processable, as current quantum computers are limited in computation capacity. Thus, quantum program developers have to consider trade-offs between accuracy (i.e., probabilistically correct functionality) and computational cost of the proposed solutions. Manually finding sufficiently accurate and efficient solutions is a challenging task, even for quantum computing experts.

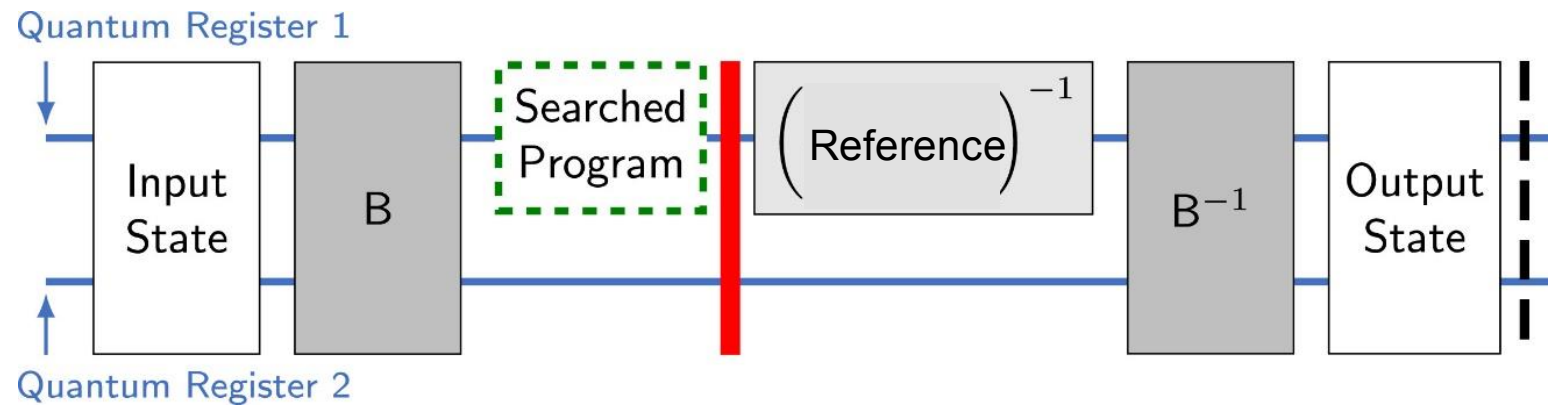
To tackle these challenges, we propose a quantum program improvement framework for an automated generation of accurate and efficient solutions, coined Genetic Quantum Program Improver (GeQuPI). In particular, we focus on the tasks of debugging and optimization of quantum programs. Our framework uses techniques from quantum information theory and applies multi-objective genetic programming, which can be further hybridized with quantum-aware optimizers. To demonstrate the benefits of GeQuPI, it is applied to 47 quantum programs reused from literature and openly published libraries. The results show that our approach is capable of correcting faulty programs and optimize inefficient ones for the majority of the studied cases, showing average optimizations of 35% with respect to computational cost.

# Preliminary: Functionally-equivalent Quantum Programs

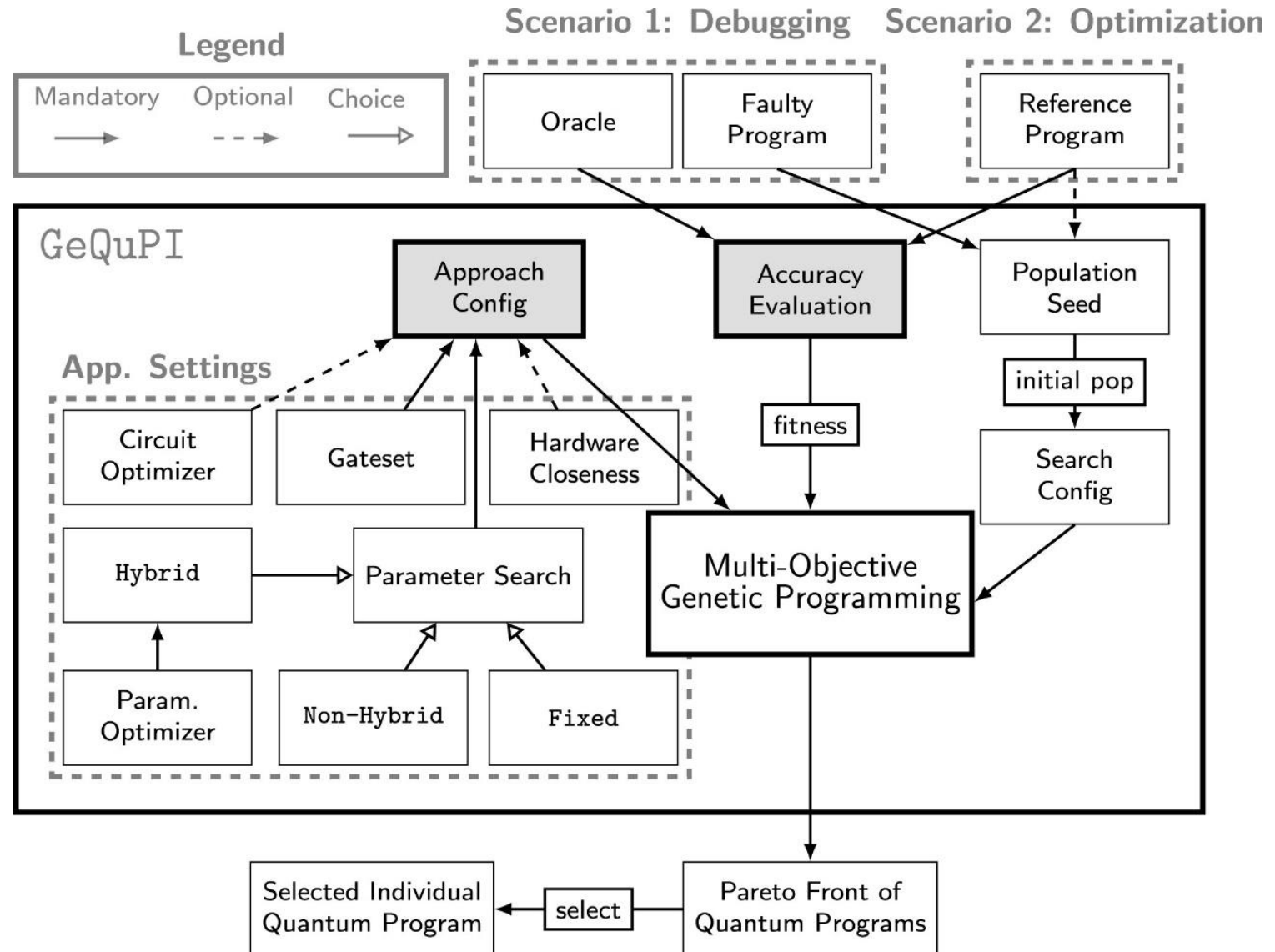
Reverse Reference and compare if  $\text{Input} == \text{Output}$  for specific input states [Burgholzer et al. 2020]



Extending to arbitrary input states using Bell-states [Mohseni et al. 2008]

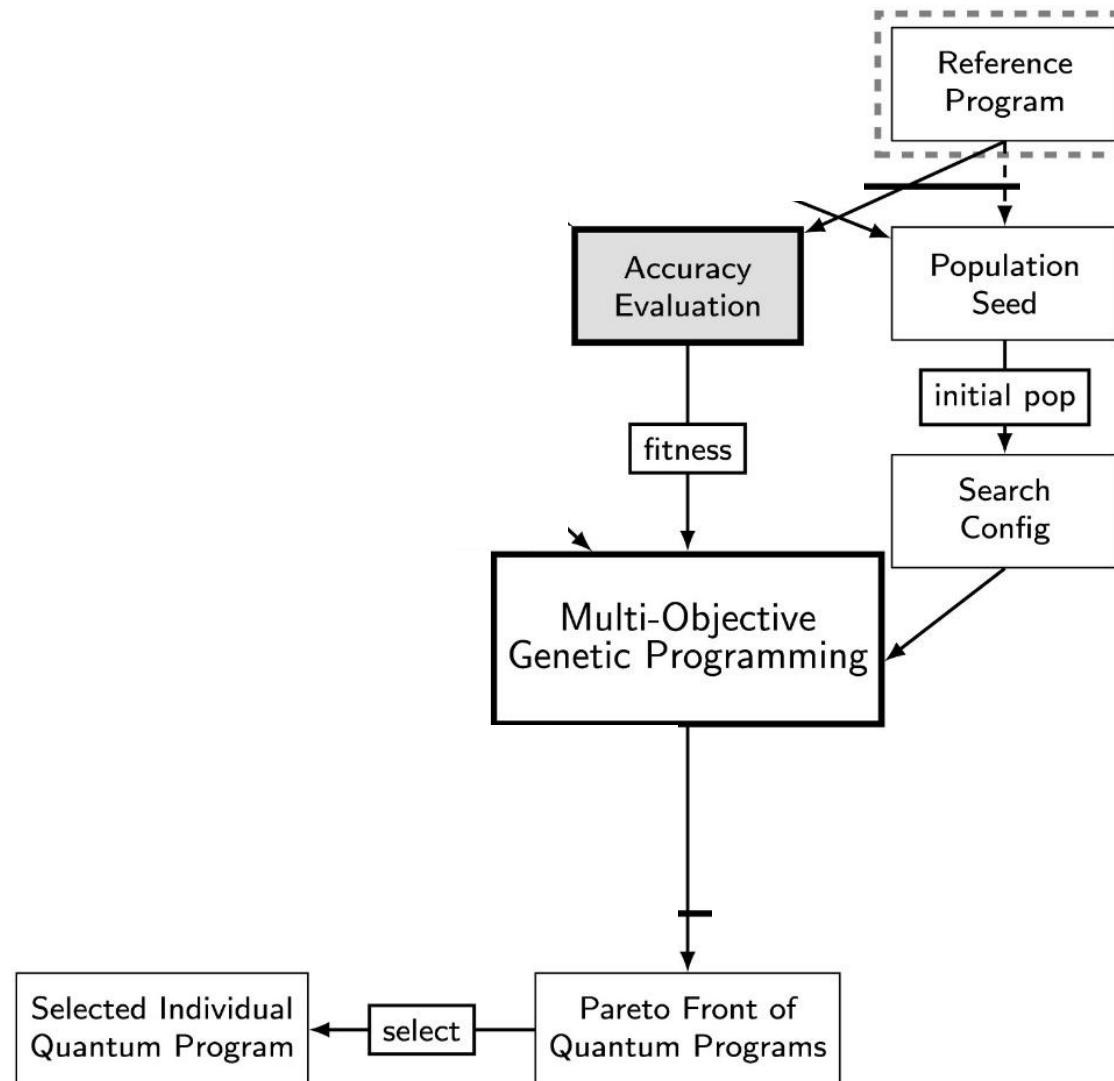


# Search Setup Overview



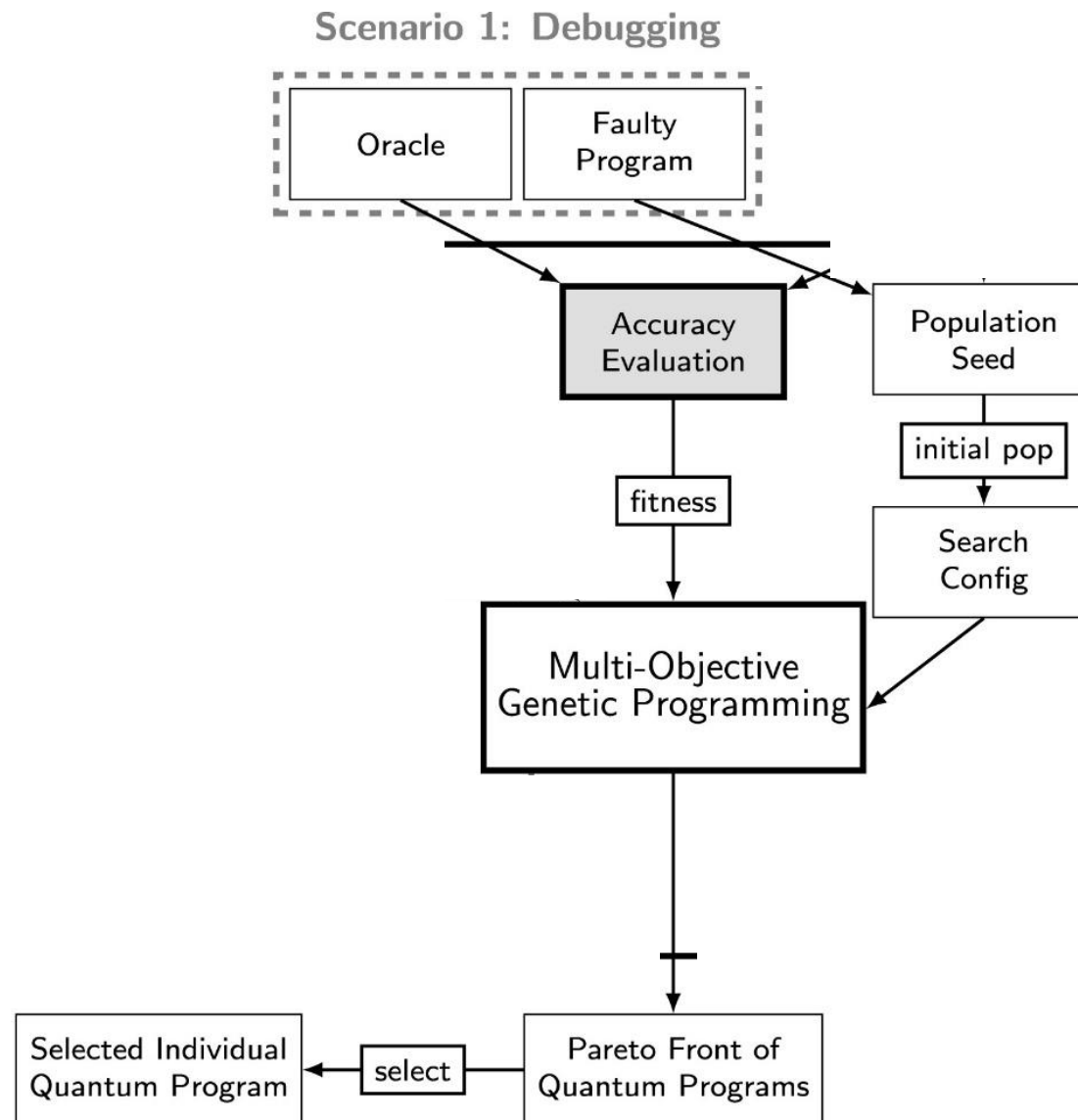
# Search Setup Overview

## Scenario 2: Optimization

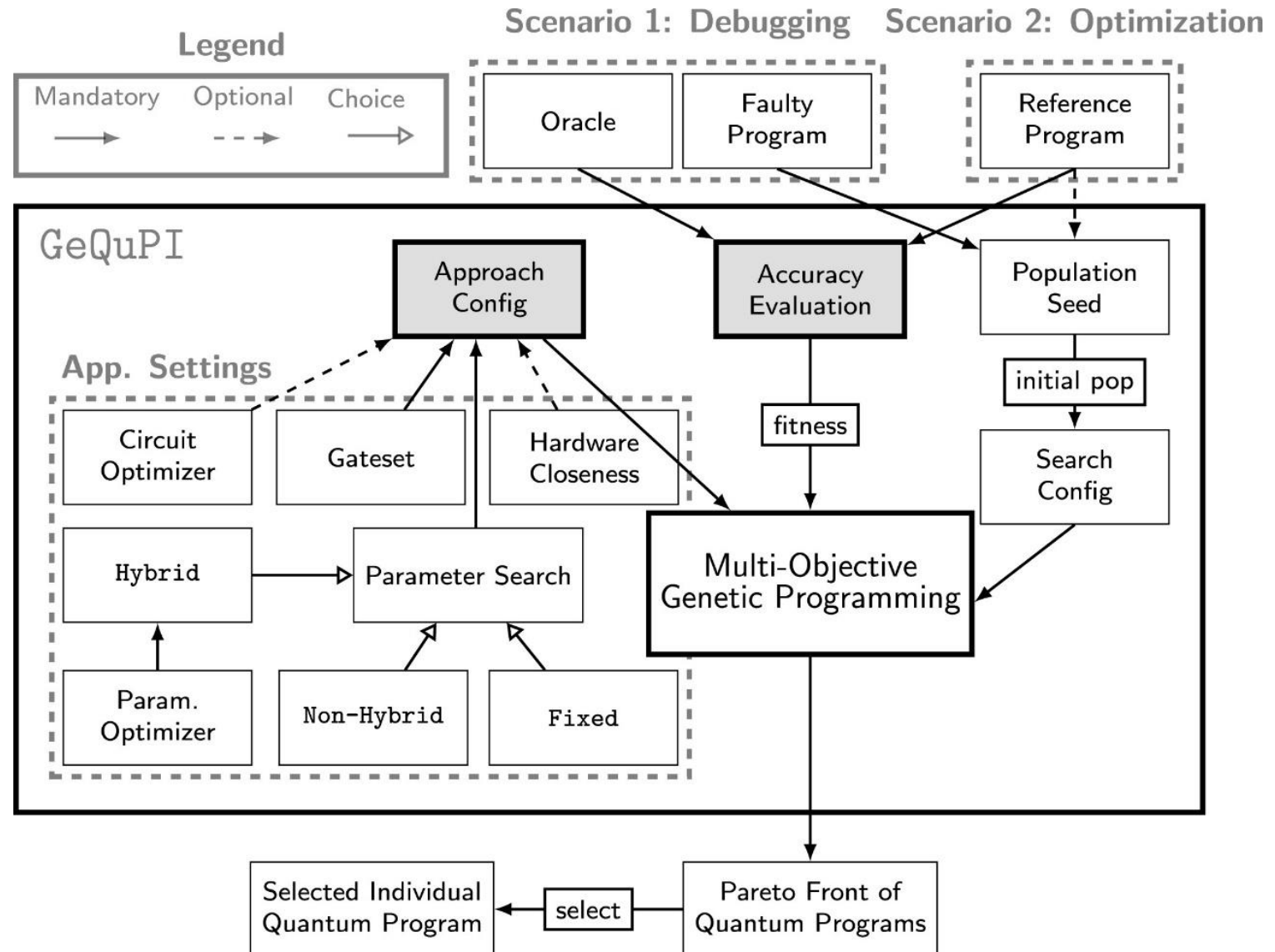




# Search Setup Overview



# Search Setup Overview



# Evaluation

- RQ1: Debugging capabilities?
- RQ2: Optimization capabilities?
- 47 quantum programs (from literature and open source projects)
  - 9 for debugging
  - 38 for optimization
- Setup
  - Genetic Algorithm: NSGA-III
  - Hybrid: 150 gen @ 40 pop
  - Non-Hyb / Fixed: 1600 gen @ 100 pop

# RQ1: Debugging capabilities?

- Hybrid can optimize
  - for specific input states
  - with Non-Hybrid & Fixed sometimes only equally good solutions are found
- Hybrid can repair arbitrary input-state programs
  - Non-Hybrid & Fixed have problems

Debugging capabilities: number of runs per category and use case.  
(Hybrid / Non-Hybrid / Fixed).

(a) RQ1.1 (Perfect Accuracy)

Input state	Problem	Optimized	Pareto Equal	Worse	Faulty
Specific	QG_8 (2 qubits)	30/30/30	0/0/0	0/0/0	0/0/0
	QSO_6 (2 qubits)	26/0/0	4/30/30	0/0/0	0/0/0
	QSO_5 (3 qubits)	30/30/30	0/0/0	0/0/0	0/0/0
	QSE_15 (4 qubits)	30/30/30	0/0/0	0/0/0	0/0/0
	QSE_3 (5 qubits)	30/30/30	0/0/0	0/0/0	0/0/0
Arbitrary	QSE2_2 (2 qubits)	30/0/0	0/0/30	0/16/0	0/14/0
	QSE2_3 (3 qubits)	0/0/0	17/0/0	8/0/8	5/30/22
	QSE2_4 (4 qubits)	0/0/0	0/0/0	7/0/0	23/30/30
	QSE2_5 (5 qubits)	0/0/0	0/0/0	6/0/0	24/30/30

# RQ2 – Optimization capabilities?

- All approaches can optimize
- Hybrid performs (almost) consistently better
- Hybrid improves by 35%
  
- Compared to “standard approach” (Qiskit built-in optimizer):
  - optimize in significantly more cases
  - and higher on average

Optimization capabilities (Hybrid / Non-Hybrid / Fixed).

(a) RQ2.1 (Perfect Accuracy)

	Optimized	Pareto Equal	Worse	Faulty
Total	541/135/105	143/84/64	50/10/14	406/911/957
Specific	274/63/45	89/84/64	23/10/14	124/353/387
Arbitrary	267/72/60	54/0/0	27/0/0	282/558/570
2 qubits	135/101/90	40/30/30	19/0/0	16/79/90
3 qubits	248/17/11	37/20/2	9/7/14	66/316/333
4 qubits	120/6/2	55/32/30	14/3/0	141/289/298
5 qubits	38/11/2	11/2/2	8/0/0	183/227/236

# RQ3: Hybrid vs. Non-Hybrid vs. Fixed?

- **Unclear** results
- Hybrid is **more diverse** (DCI, HV)
- IGD+ indicates that Hybrid is **less performant**

	PI Comparison	DCI	HV	IGD+
All	Hybrid vs. Non-Hybrid	✓✓	✓	✗
	Hybrid vs. Fixed	✓✓✓	✓	≡
	Non-Hybrid vs. Fixed	✓✓	✓	≡
Repair	Hybrid vs. Non-Hybrid	✓✓✓	✓	≡
	Hybrid vs. Fixed	✓✓	✓	✓✓
	Non-Hybrid vs. Fixed	≡	≡	≡
Optimize	Hybrid vs. Non-Hybrid	✓✓	≡	✗
	Hybrid vs. Fixed	✓✓✓	✓✓	✗
	Non-Hybrid vs. Fixed	✓✓✓	✓	≡
Specific	Hybrid vs. Non-Hybrid	≡	≡	≡
	Hybrid vs. Fixed	✓✓✓	✓	≡
	Non-Hybrid vs. Fixed	✓✓✓	✓	≡
Arbitrary	Hybrid vs. Non-Hybrid	✓✓✓	✓	✗✗
	Hybrid vs. Fixed	✓✓✓	✓✓	≡
	Non-Hybrid vs. Fixed	✓	≡	≡

# RQ4: Search configurations?

(non-exhaustive assessment)

**seeding** the initial population

→ **improvements** for **optimization** and **debugging**

initial population seeding

→ **most robust** configuration wrt. scaling qubits

indication of **saturation effects** wrt. population size and number of generations

# RQ5 – Hardware-specificity?

Higher levels of **hardware specificity** improve the results

No hardware considerations performs worst

Using **transpiled programs** in the search process significantly improves the **share of optimized programs**

However, higher levels of **hardware-specific** considerations **increase the execution time**.

**transpilation** of programs **for the fitness values** only resembles a **viable balance** between solution quality and execution time



# Conclusion & Future Work

SBSE in general is applicable for QSE

- *What is the best instantiation for QSE?*

Hybrid search seems beneficial

- *What is the best way to integrate different searchers?*

Can be applied on different abstraction levels

- *How much do we have to know about the execution?*

Seeding makes results more robust for improvement

- *How much diversity do we lose?*

# Ongoing Work

Caching possibilities in search processes

- Reuse similarities within individuals to improve simulation speed

Encoding intuition in search

- E.g. „my circuit requires entanglement“

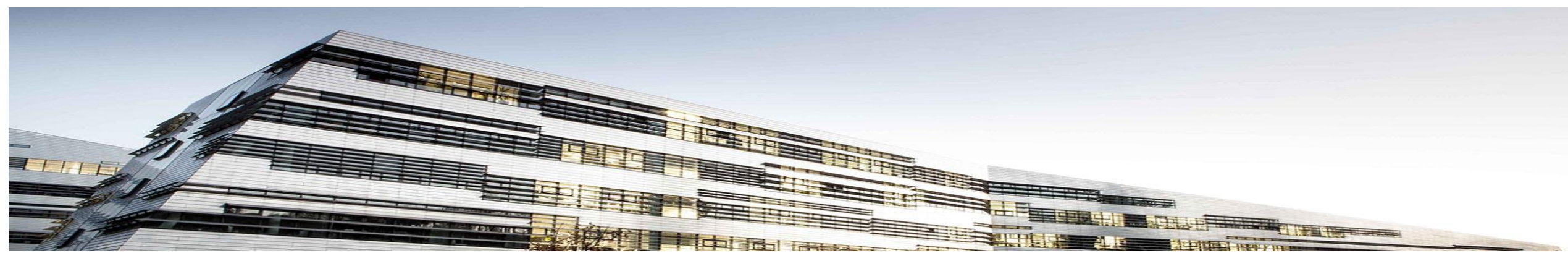
Alternative optimization approaches

- Reinforcement learning, ...

Alternative encodings

- Change-based encodings with MOMoT





**Thank you!**  
**Comments? Questions? Feedback?**

**Looking forward to discussions and collaborations!**

**Tooling/data available at:**

<https://github.com/jku-win-se/Genetic-Programming-for-Quantum-Operator-Discovery>

<https://github.com/jku-win-se/QImprove>